**CS 412, HW #1**

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**Question 1.**

**1.1 Answers**

*A) Maximum and minimum.*

Mid-Term 37 , 100

Final: 35 , 100

*B) First quartile Q1, median, and third quartile Q3*

Mid-Term: 68.0 , 77.0 , 87.0

Final: 82.0 , 89.0 , 96.0

*C) Mean*

Mid-Term: 76.715

Final: 87.084

*D) Mode*

Mid-Term: 77 83

Final: 97

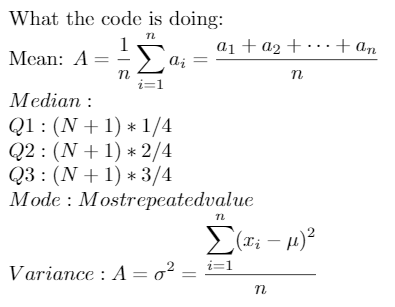
*E) Variance*

Mid-Term: 173.10577

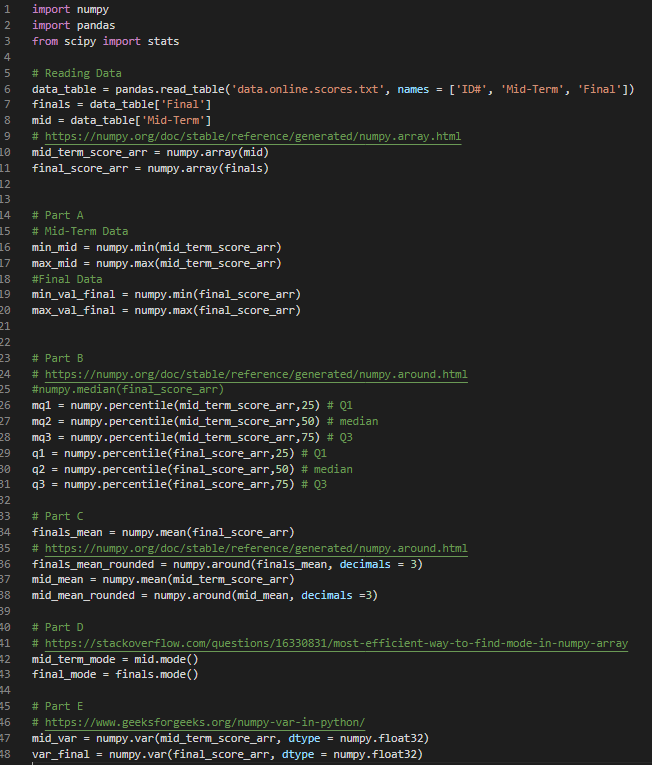
Final: 119.11294

**1.2 Explanation and Equations**

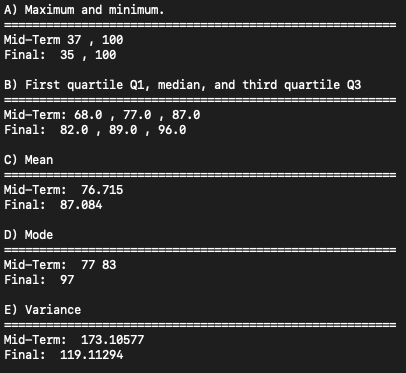
1. Numpy was used to find min and max
2. Numpy’s function percentile() was used. 25,50,75 for Q1, Q2, and Q3 relatively.
3. Numpy’s function mean() was used.
4. Numpy’s function mode()
5. Numpy’s function var() was used.

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**1.3 Code (Not including print statements)**

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**1.4 Terminal Output**



**Question 2.**

**2.1 Answers**

**A) Compute and compare the variance of midterm-original and midterm-normalized, i.e., the midterm scores before and after normalization.**

Variance MidTerm: 173.10577

Normalized Variance: 1.0

**B) Given an original midterm score of 90, what is the corresponding score after normalization?**

Mean: 76.715

Std-Dev: 13.156966785699508

Using v' = v - Avg / std-dev

Our score of 90 is normalized to 1.009731210573523

**C) Compute the Pearson’s correlation coefficient between midterm-original and finals-original?**

Pearson’s correlation coefficient: 0.544424742312412

**D) Compute the Pearson’s correlation coefficient between midterm-normalized and finals-original.**

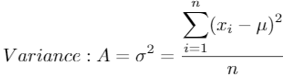
Pearson’s correlation coefficient: 0.544424742312412

**E) Compute the covariance between midterm-original and finals-original.**

Covariance: 78.25419419

**2.2 Explanation and Equations**

1. Numpy var() was used. The function performed the following equation:



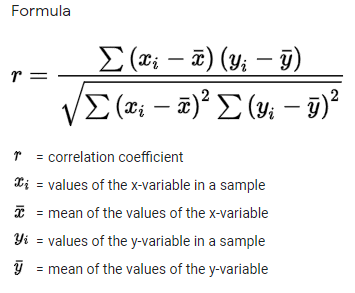
Using the standard dev and mean. I used the same equations as I did in question 1 to find those.

1. Scipy zscore() was used

then using v' = v - Avg / std-dev, we normalize the score

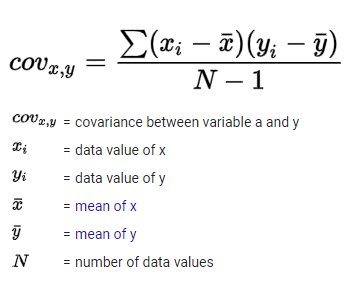
1. Scipy pearsonr() was used
2. Scipy pearsonr() was used

For both C and D the pearsonr() function utilized the following equation.

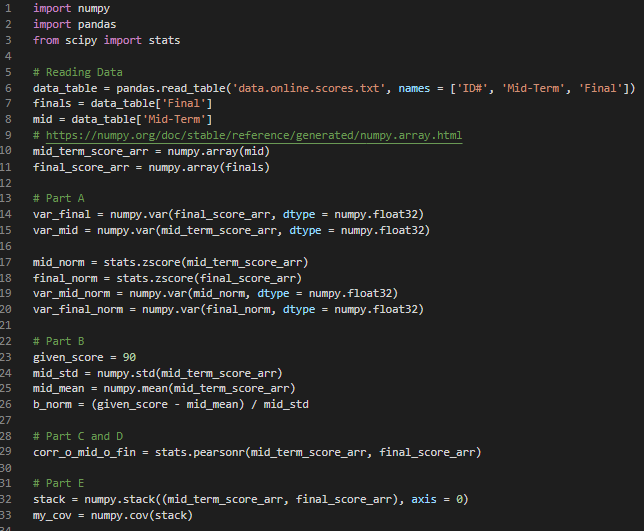


1. Numpy’s stack() was used

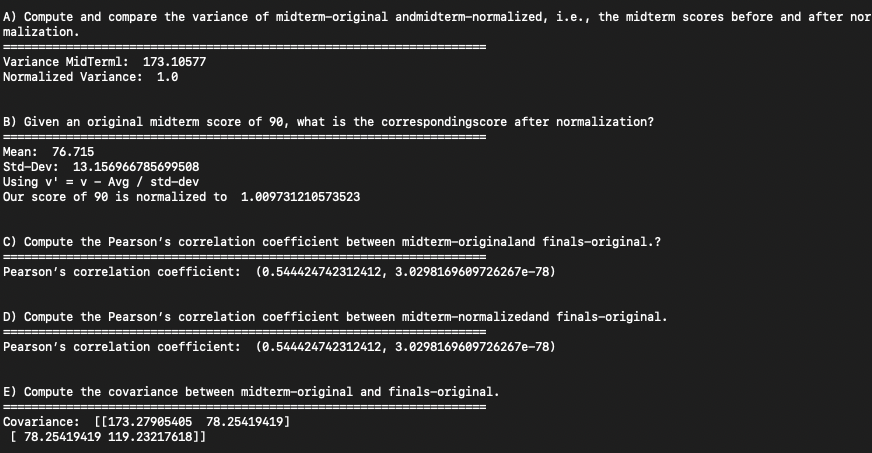
This allowed me to find covariance. I could have use the cov() function in Panda, but this worked just as fine. It utilized this equation.



**2.3 Code (Not including print statements)**

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**2.4 Terminal Output**



**Question 3.**

**3.1 Answers**

**a) Each library has multiple copies of each book. Based on all the books (treat**

**the counts of the 100 books as a feature vector for each of the libraries), compute the**

**Minkowski distance of the vectors for CML and CBL with regard to different h values:**

i) 6152.0

ii) 715.3278968417211

iii) 170.0

**b) Compute the cosine similarity between the feature vectors for CML and CBL.**

Cosine similarity: 0.8414040256623079

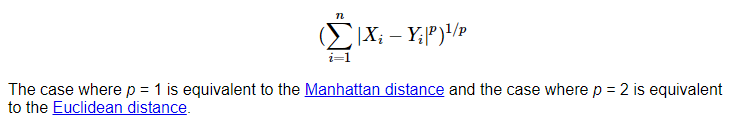
**c) Compute the Kullback-Leibler (KL) divergence between CML and CBL**

KL(CML || CBL): 0.207 -> 20.7%

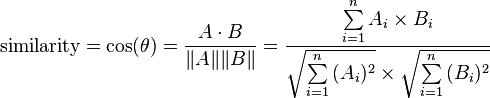
KL(CBL || CML): 0.2294 -> 22.94%

**3.2 Explanation and Equations**

a) Using scipy library and used minkowski() function.

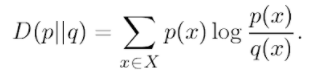
****Based on equation above, this would have been calculated without any specific function. Rather by manual calculation. We could have found difference of CBL and CML data, taken their absolute value and summed these differences together. The p \* 1/p cancels out. And thus, we are left with the original equation showed above. The function had the following parameters, (vector 1, vector 2, h value). Thus, for parts i, ii, and iii I simply changed the h value that was given. For part iii, I used float(‘inf’)

b) For this part, I again, used scipy, however, this time I used the cosine distance function.



I could have simply used this equation, but using the predefined function allowed for a much cleaner code base.

c) KL divergence could have been found using SK-Learns lib, however, I used entropy in numpy. When scipy.stats.entropy is used, it will normalize the probabilities to one. Scipy's entropy function will calculate KL divergence if feed two vectors p and q, each representing a probability distribution. If the two vectors are not pdfs, it will normalize them first.



Using the equation shown above, we could ‘manually’ calculate this.

**3.3 Code (Not including print statements)**

**Text

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**3.4 Terminal Output**

Text

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**Question 4.**

**4.1 Answers**

**a) Calculate the distance between the binary attributes Buy Beer and Buy Diaper**

**by assuming they are symmetric binary variables.**

Distance: 0.015691868758915834

**b) Calculate the distance between the binary attributes Buy Beer and Buy Diaper**

**by assuming they are symmetric binary variables.**

Jaccard Coefficient : 0.7317073170731707

**c) Compute the χ2 statistic for the contingency table.**

χ2: 2450.716326822006

**d) Consider a hypothesis test based on the χ2 statistic where the null hypothesis**

**is that Buy Beer and Buy Diaper are independent? Can you reject the null hypothesis?**

***at a significance level of α = 0.05? Explain your answer, and mention the degrees***

***of freedom used for the hypothesis test.***

If the value was more than 0.05 we could not reject the null hypothesis

The value based on info given was: 0.0

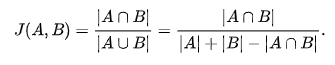
We were able to reject

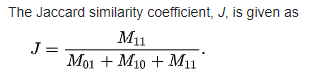
P value: 0.0

Deg of freedom: 1

**4.2 Explanation and Equations**

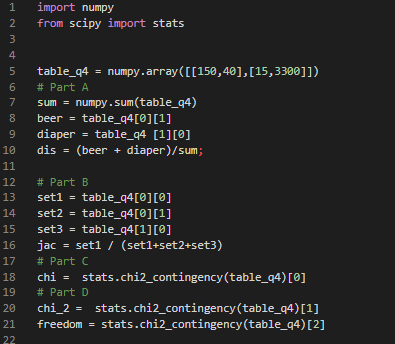
1. This was done without using any library. First, I added the items then I divided by the sum of the entire array.
2. The Jaccard Coefficient between buying beer and diaper was done with this equation.

Which translates to

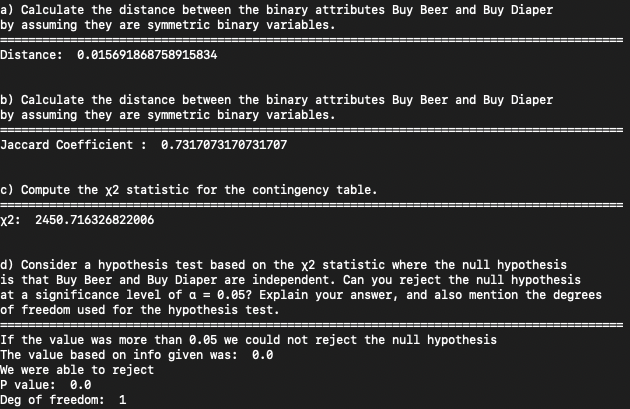


1. Done with the use of scipy chi2\_contigency()
2. Done with the use of scipy chi2\_contigency()

**4.3 Code (Not including print statements)**

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**4.4 Terminal Output**

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